

Solar Polar Fields During Cycles 21 — 23: Correlation with Meridional Flows

P. Janardhan¹ K.B. Susanta¹ S. Gosain^{1,2}

¹ Physical Research Laboratory, Astronomy & Astrophysics Division, Navrangpura, Ahmedabad - 380 009, India.

email: jerry@prl.res.in email: susanta@prl.res.in

² Udaipur Solar Observatory, P.O. Box 198, Dewali, Udaipur 313001, India.

email: sgosain@prl.res.in

Abstract

We have examined polar magnetic fields for the last three solar cycles, *viz.*, cycles 21, 22 and 23 using NSO Kitt Peak synoptic magnetograms. In addition, we have used SoHO/MDI magnetograms to derive the polar fields during cycle 23. Both Kitt Peak and MDI data at high latitudes (78° – 90°) in both solar hemispheres show a significant drop in the absolute value of polar fields from the late declining phase of the solar cycle 22 to the maximum of the solar cycle 23. We find that long term changes in the absolute value of the polar field, in cycle 23, is well correlated with changes in meridional flow speeds that have been reported recently. We discuss the implication of this in influencing the extremely prolonged minimum experienced at the start of the current cycle 24 and in forecasting the behaviour of future solar cycles.

Introduction

Detailed studies of solar magnetic features is an important area of research because solar magnetic fields have a profound and far reaching influence on the earth's near-space environment. With mankind's increased dependance on space based technology, much of which is at risk due to solar activity that waxes and wanes with the sunspot cycle, it is imperative that we understand the solar magnetic cycle and its effects on the near-space environment. In addition, due to the significant anthropogenic influence on climate change in recent times, it is becoming increasingly important to distinguish and delineate the degree to which the solar cycle can affect terrestrial climate.

The evolution of large scale solar magnetic fields is attributed to a solar magnetohydrodynamic dynamo operating inside the sun which involves three basic processes *viz.* the generation of toroidal fields by shearing pre-existing poloidal fields (the Ω effect); the regeneration of poloidal fields by twisting toroidal flux tubes (the α effect); and finally, flux transport by meridional circulation to carry background magnetic fields poleward from the equator Parker (1955a,b); Steenbeck and Krause (1969); Wang, Sheeley, and Nash (1991); Choudhuri, Schussler, and Dikpati (1995); Dikpati and Charbonneau (1999).

With the measurement of the sun's polar field Babcock and Babcock (1955) and the subsequent proposal of polar field reversal during maximum of each solar cycle Babcock (1959), research in

solar magnetic fields and its effect on subsequent cycles was channeled in a new direction. Since then many investigations have been carried out to explore the relation between evolution of large-scale magnetic fields and their association with polar field structures Fox, McIntosh, and Wilson (1998); Benevolenskaya, Kosovichev, and Scherrer (2001, 2002); Gopalswamy *et al.* (2003)).

The current sunspot minimum that we have seen at the end of cycle 23 have been one of the deepest minima that we have experienced in recent times with roughly 71%—73% of the days in 2008 and 2009 respectively being entirely spotless. Apart from this, cycle 23 has shown several other peculiarities, like a second maximum during the declining phase that is unusual of odd numbered cycles, a slower rise to maximum than other odd numbered cycles and a slower than average polar reversal. Such departures from “*normal*” behaviour need to be studied and understood as they could be significant in the context of understanding the evolution of magnetic fields on the sun.

In this paper, we have examined the solar polar field behavior for the last few cycles and the following sections will discuss our findings.

Magnetic Field Data

Low resolution NSO/Kitt Peak data

Magnetic field data is available as standard FITS format files from the National Solar Observatory, Kitt Peak, USA (NSO/Kitt Peak) synoptic magnetogram database (<ftp://nsokp.nso.edu/kpvt/synoptic/mag/>). These synoptic maps are in the form of 180×360 arrays starting from Carrington Rotation (CR) number CR1625 through CR2006 corresponding to years 1975.13 through 2003.66. For the period covering the years from 2003.66 through 2009.11, synoptic maps were obtained from the Vector Spectro Magnetograph (VSM) of the NSO Synoptic Optical Long-term Investigations of the Sun (SOLIS) facility for solar observations over a long time frame (NSO/SOLIS) (<ftp://solis.nso.edu/synoptic/level3/vsm/merged/carr-rot/>). A few data gaps during CR1640-CR1644, CR1854, CR1890, CR2015, CR2016, CR2040 and CR2041 were filled in by interpolated values while making the plots.

The resolution of the synoptic maps is 1° in both longitude (1° to 360°) and latitude (-90° to 90°). A typical Carrington synoptic map is produced from full disk magnetograms spanning over an entire Carrington rotation period. Each individual magnetogram is first remapped into latitude and longitude coordinates and then added together to produce the final synoptic map for each CR. All synoptic magnetogram maps, represented as an $i \times j$ data array with i and j representing the latitude and longitude respectively, for any given CR number n , contain magnetic flux density $\phi_{i,j,n}$, in units of Gauss averaged over equal areas of the sun. The actual flux units are then obtained by multiplying by the appropriate area.

Since we are interested in the variation of photospheric magnetic fields with latitude, data is processed by taking longitudinal averages for each latitude bin of 1° by converting the data to a one dimensional array of 1×180 . Any latitude element i , for a given CR, n will contain the averaged magnetic field represented by equation (1).

$$\phi_{i,n} = \frac{\sum_{j=1}^{360} \phi_{i,j,n}}{360} \quad (1)$$

Now, the averaged magnetic field for a range of latitudes in any CR is obtained by averaging $\phi_{i,n}$ as shown by equation (2).

$$\phi_n = \frac{\sum_{i=k}^p \phi_{i,n}}{p - k} \quad (2)$$

Where k and p are the row numbers corresponding to a latitude bin. Using the above procedure, we have obtained average magnetic fields in each solar hemisphere for three different latitude bins between ranges

- 0° and 45° – representing the equatorial or toroidal fields;
- 45° and 78° – representing the mid latitude fields;
- and 78° and 90° – representing polar fields in each hemisphere.

High resolution MDI Data

Line-of-sight magnetograms from the Michelson Doppler Interferometer (MDI, Scherrer *et al.* (1995)) onboard the Solar and Heliospheric Observatory (SoHO; Domingo, Fleck, and Poland (1995)), are available from 1996 onwards. High resolution (3600×1080 pixels) MDI synoptic images beginning from CR1911 through CR2080 are used, with data gaps for CR1938-CR1942, CR 1945 and CR2073. It must however be noted that there are occasions when the inclination of the earth's orbit to the helioequator will cause one of the poles of the sun to not be clearly visible. We have used MDI synoptic magnetogram available at <http://soi.stanford.edu/magnetic/index6.html> that have been corrected for this effect.

Since MDI measurements are considered to be more reliable than Kitt-Peak observations, we have compared the two data sets for the period after 1996 to check if the results agree with each other. Also, data gaps when present, for example from CR1938 to CR1941 were dealt with by replacing them with interpolated values, and these have been indicated in the figures. Finally, the resolution of the MDI data was degraded (by averaging) to the resolution of the NSO/Kitt Peak data so as to be able to compare the results. It may be noted that for the MDI data, only the latitude bin between 78° and 90° was considered.

Magnetic Field Measurements

As mentioned earlier, meridional circulation is the primary poloidal flux transport agent in the sun. A poleward meridional flow at the solar surface has been shown to exist, with average speeds in the range 10 m s^{-1} – 20 m s^{-1} Duvall (1979); Hathaway (1996); Hathaway *et al.* (1996). Since the amplitude of this surface flow is more than an order of magnitude weaker than other surface flows like granulation, supergranulation and differential rotation, the effects of this meridional circulation can be best studied at high solar latitudes where the modulation due to the solar cycle is negligible or absent. Figure 1 shows the measurements of the magnetic field in each solar hemisphere as a function of time in years in the two latitude ranges 0° – 45° and 45° – 78° . While the upper two panels of Fig. 1 show the absolute value of the field in the latitude range 0° – 45° for the northern and southern hemisphere respectively, the lower two panels show the absolute value of the magnetic field in the latitude range 45° – 78° for the northern and southern hemisphere respectively. The filled dots represent the actual measurements derived from the NSO/Kitt Peak data base, while the solid line is a smoothed curve representing the data. The vertically oriented dashed parallel lines demarcate cycles 21, 22 and 23. It can be seen from Fig. 1 (upper two panels) that there is a strong solar cycle modulation present in the latitude range $\pm 0^\circ$ – $\pm 45^\circ$ while the solar cycle modulation is much weaker and barely discernable in the latitude range $\pm 45^\circ$ – $\pm 78^\circ$ for cycles 21 and 22 while it is not seen for cycle 23.

Figure 2 shows the actual (signed) measurements of magnetic field, in each solar hemisphere, as a function of time in years in the latitude range 78° – 90° . While the upper panel of Fig. 2 show

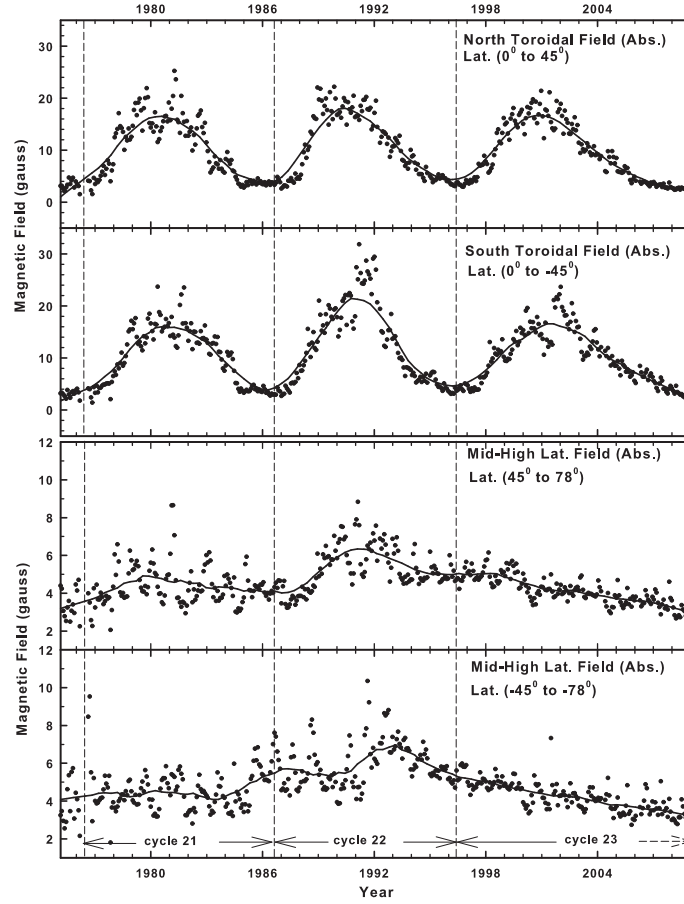


Figure 1: The four panels, in pairs starting from the top, show the variations in the magnetic field in the north and south solar hemisphere respectively, as a function of years for the solar cycles 21–23. The absolute value of the magnetic field in the latitude range 0° – $\pm 45^\circ$ is shown in the first pair of panels while the second pair of panels show the absolute value of magnetic field in the latitude range 45° – 78° . The filled dots represent the actual measurements while the solid line is a smoothed curve. The vertically oriented dashed parallel lines demarcate cycles 21, 22 and 23 respectively.

the actual (signed) value of the field for the northern hemisphere, the lower panel shows the actual (signed) value of the magnetic field for the southern hemisphere. The filled dots, with 1σ error bars, represent the measurements derived from the NSO/Kitt Peak data, while the solid blue line is a smoothed curve. Points where data gaps were filled by interpolation are shown by red dots. The vertically oriented dashed parallel lines demarcate cycles 21, 22 and 23. A comparison of the the polar field during cycles 22 and 23 from Fig. 2 shows that the longitude averaged polar magnetic field between $\pm 78^\circ$ – $\pm 90^\circ$ during the current extended minimum leading up to the current cycle 24 is weaker than the corresponding minimum period in cycles 21 and 22. Also, a comparison of the fields in the two hemispheres, in cycle 23, shows that the south polar field is weaker than north polar field. In a detailed analysis of sunspot data and longitude-averaged photospheric magnetic flux Dikpati *et al.* (2004) has also pointed out several peculiarities during cycle 23 like the slow build up of the polar field after the occurrence of the polar field reversal, the asymmetry in polar reversal for north and south pole and the steady behavior of the north polar field in comparison to south polar field from the late declining phase of cycle 22 to early rising phase of cycle 23. All of these features can also be clearly

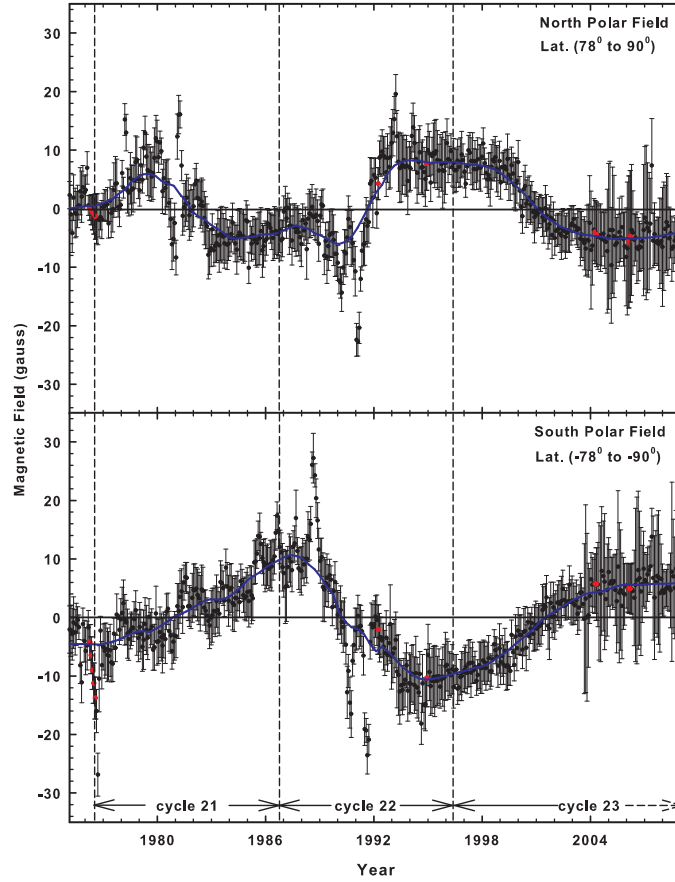


Figure 2: The panels show the variations in the magnetic field in the north (upper panel) and south solar hemisphere (lower panel) as a function of years for the solar cycles 21–23. The actual (signed) magnetic field in the latitude range 78° – 90° is shown in the two panels. The filled dots, with 1σ error bars represent the actual measurements while the blue solid line is a smoothed curve. The vertically oriented dashed parallel lines demarcate cycles 21, 22 and 23 respectively. Points where data gaps were filled by interpolation are shown by red dots.

seen in Fig. 2 for the period of cycle 23.

The two panels of Figure 3 show the variation in the absolute value of the polar magnetic field in the latitude range 78° – 90° for the north and south solar hemisphere as a function of years for the solar cycles 21–23. During cycle 23, MDI data is shown by red dots for comparison between NSO/Kitt Peak data and MDI data. Marked by green dots are points where MDI data gaps were filled in by interpolation. It may be noted that the MDI high resolution data was reduced, by averaging, to that of the NSO/Kitt Peak data for comparison. A striking feature in Fig. 3 is a steep and continuous drop of the average polar field (in both NSO and MDI data) from the late declining phase of cycle 22 to the maximum of cycle 23 in both the hemispheres. A slow continuous drop of ~ 13 G from 1994 to 2001 is seen in the northern hemisphere while a sharp continuous drop of ~ 9 G from 1995 to 2002 is seen in the southern hemisphere. Cycles 21 and 22 however showed no such drop. The recent and extended minimum at the end of cycle 23 is also interesting in that the average polar field behavior showed no variation and remained steady from 2004 onwards in both the hemispheres as seen from both NSO and MDI data. The MDI data however is systematically lower than the NSO/Kitt Peak

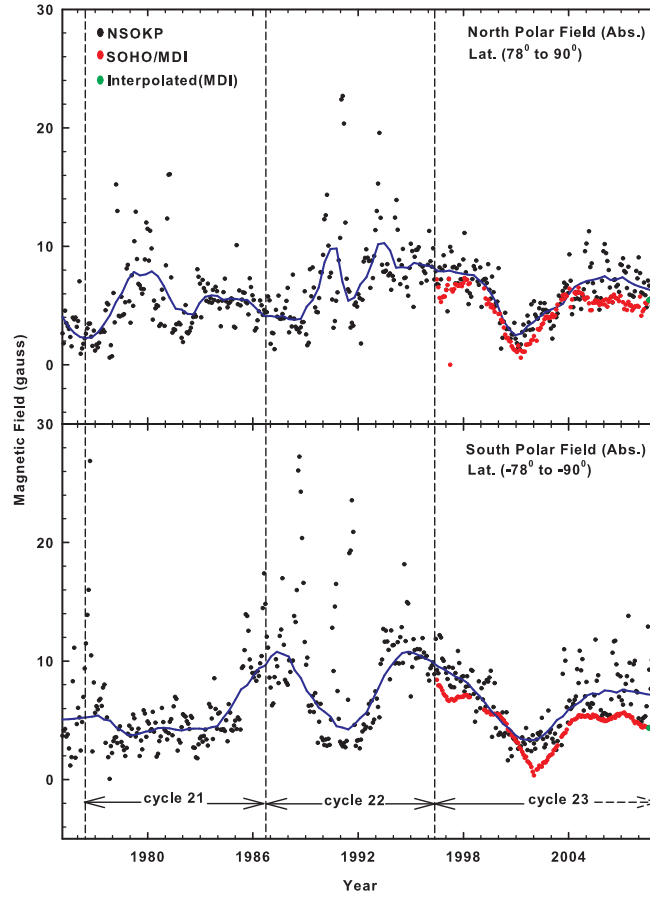


Figure 3: The two panels show the variations in the absolute value of the polar magnetic field in the latitude range 78° – 90° for the north and south solar hemisphere as a function of years for the solar cycles 21–23. The actual measurements derived from the NSO/Kitt peak data base is shown by filled dots while the blue solid line is a smoothed curve. MDI data for cycle 23 (for comparison) is shown by red dots. The vertically oriented dashed parallel lines demarcate cycles 21, 22 and 23 respectively. Points where MDI data gaps were filled by interpolation are shown by green dots.

values throughout cycle 23.

Polar Fields and Meridional Flow Speeds

Cycle 23

The sun's meridional flow which is directed poleward at the surface of the sun, is an axis symmetric flow of the order of 10 – 20 m s^{-1} . This meridional flow is responsible for carrying background magnetic fields poleward from the equator and plays an important role in determining the strength of the solar polar field and the intensity of sunspot cycles Hathaway and Rightmire (2010). There have been some attempts to infer surface meridional flow speeds using the helioseismic technique of ring-diagram analysis applied to MDI data Haber *et al.* (2002). However, a more recent and detailed study using MDI images of the line-of-sight magnetic fields Hathaway and Rightmire (2010) has reported measurements of the surface meridional flow speed in the latitude range $\pm 75^\circ$ in cycle 23.

These measurements have shown a lot of variation in the meridional flow speeds in cycle 23. These authors determined a meridional flow speed of 11.5 m s^{-1} at minimum of cycle 23 in 1996 — 1997 which then dropped to 8.5 m s^{-1} at the maximum in 2000 — 2001. It must be noted here that this drop in the flow speed coincides with the steep drop in the absolute value of the magnetic field that is seen in both the NSO/Kitt-Peak and MDI data (see Fig. 3). In fact, the MDI data in the southern hemisphere continues to drop until 2002 after which it rises again. Between 2001 and 2004, the measured meridional flow speed again increased to 13.0 m s^{-1} and remained constant at this value thereafter. Again, from Fig. 3 we can see a corresponding steep increase in the absolute value of the polar field between 2001 and 2004. After this the absolute value of the magnetic field remains constant in both hemispheres until 2009. From Fig. 3 it is clear that the polar field strength since 2004, as seen by both NSO/Kitt Peak and MDI has remained constant. Figure 4 shows a comparison be-

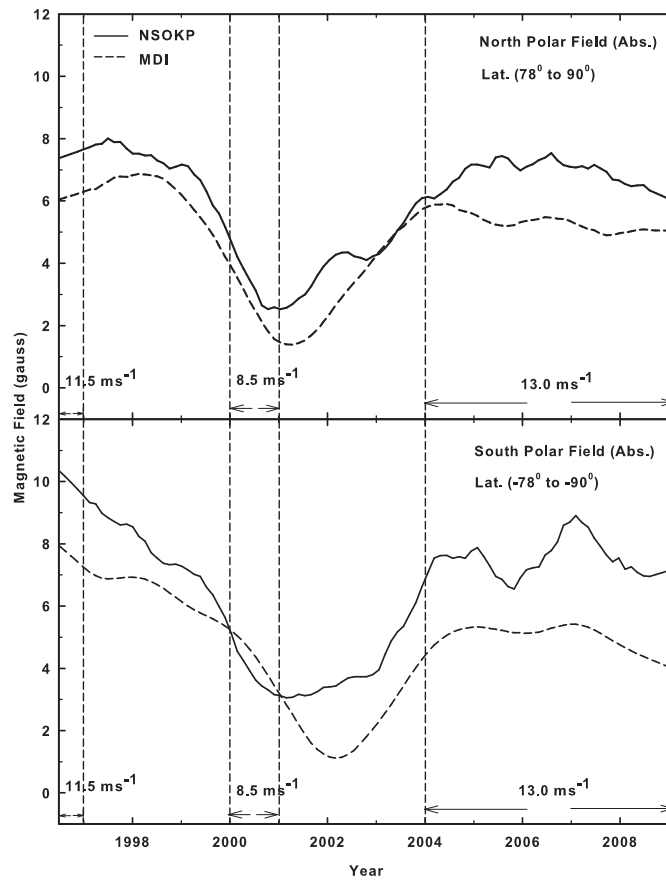


Figure 4: The two panels show a comparison between Kitt-Peak/NSO data and MDI data in cycle 23 for the two hemispheres. The Northern hemisphere is shown in the upper panel while the southern hemisphere is shown in the lower panel. The meridional flow speeds as reported by Hathaway & Rightmore (2010) have been indicated by vertically oriented dashed parallel lines.

tween the averaged absolute magnetic fields determined from NSO/Kitt Peak synoptic magnetogram maps and MDI synoptic magnetogram maps for the northern (upper panel) and southern (lower panel) hemispheres for solar cycle 23. While the solid line is a smoothed curve representing the NSO data, the dashed line is a smoothed curve representing the MDI data. The meridional flow speeds as reported by Hathaway and Rightmire, 2010 are indicated at the bottom of each panel and demarcated

by vertically oriented dashed parallel lines. It may be noted again that the MDI high resolution data (3600×1080 pixels) was averaged and reduced to that of the NSO/Kitt Peak data (360×180 pixels) for comparison. The recent and extended minimum at the end of cycle 23 is also interesting in that the average polar field behavior showed no variation and remained steady from 2004 onwards in both the hemispheres as seen from Figure 4. The magnetic field of MDI data however is systematically lower than the NSO/Kitt Peak values throughout cycle 23 and in the southern hemisphere, the MDI data shows a steep drop between 1997 – 2002.

Strength of upcoming solar cycle 24

In trying to predict the strength of future solar cycles, magnetic persistence or the sun's memory of the polar field strength at minimum in the previous cycle has been postulated as the influencing factor. Some authors have used this method to try and predict the strength of upcoming of cycles through magnetic persistence or Sun's memory (Schatten *et al.* (1978); Layden *et al.* (1991); Schatten and Sofia (1996)). Later, it was postulated that magnetic persistence is itself governed by meridional flow speed (Hathaway (1996); Haber *et al.* (2002); Basu and Antia (2003)) with slower meridional flows resulting in longer memory. In addition, a slower meridional flow speed would also determine the cycle period.

Two different views were postulated to predict the strength of solar cycle 24. The first predicted the new solar cycle 24 to be a strong cycle compared to cycle 23 Dikpati, de Toma, and Gilman (2006). These authors used sunspot area of last three cycles based on flux transport dynamo model as the source term for generating poloidal field. The second predicted the new solar cycle 24 to be weak one Choudhuri, Chatterjee, and Jiang (2007). These authors used only inputs from the last solar cycle since the generation of poloidal fields involved randomness and indeterministic behavior.

Discussion and Conclusions

Though a great deal of progress has been made in our understanding of meridional flows and their role in determining the strength of the polar field and the amplitude of the following cycles, there seems to be a basic disagreement between flux transport dynamo models and surface flux transport models. Fast meridional flows, in the flux transport dynamo models, produce stronger polar fields and a short cycle, as compared to the observations of surface flux transport which give rise to weak polar fields and a long solar cycle. While the dynamo models have fields of one polarity centered on the sunspot latitudes, surface models have bands of opposite magnetic polarity on either side of the sunspot latitudes. The cause for the difference in these two models, arises mainly due to the above difference in the latitudinal distribution of magnetic polarities and has been adequately explained by Hathaway and Rightmire (2010).

We have seen from our data, a large and unusual drop in the absolute value of the polar fields during cycle 23 compared to previous cycles (section) and also its association with similar behavior in meridional flow speed (subsection). In addition, Hathaway and Rightmire (2010) has shown that the meridional flow generally shows a decrease from minimum to maximum. This has also been reported for previous solar cycles Komm, Howard, and Harvey (1993) with less certainty and poorer time resolution than for cycle 23 where, high resolution MDI data is available. The minimum leading up to the start of cycle 24 has been very deep and prolonged and we have seen that the corresponding polar fields have been at their lowest compared to the other cycles 21 and 22. We believe that the memory of this very weak polar field in cycle 23 is the cause of the extended solar minimum we have witnessed. Since the sun's memory depends on polar field strength we believe that the upcoming

cycle 24 will be a much weaker cycle compared to cycle 23 which is in accordance with the later prediction proposed by Choudhuri, Chatterjee, and Jiang (2007).

We have seen above that the absolute value of the polar magnetic field in the latitude bin 78° – 90° virtually mirrors the change in the meridional flow speeds in cycle 23, with meridional flow speeds dropping when the absolute value of the field drops. Unlike cycles 21 and 22, the absolute values of the polar magnetic fields in cycle 23 showed similar trends in both hemispheres. Since high resolution MDI data is available only from 1996, it is not possible to compute meridional flow speeds during cycles 21 and 22. However, it may be noted that in both cycles 21 and 23, the behaviour of the absolute value of the polar fields is different in each hemisphere. If we assume that the correlation between the absolute value of the polar fields and the meridional flow velocities holds good for all solar cycles, then this would imply that the field reversals occurred at different times in the two hemispheres in both cycles 21, 22 and 23.

The study of polar magnetic fields can thus provide a good clue on the nature of the meridional flows in each hemisphere. Such inputs would be important in predicting the behaviour of the future solar cycles. In addition to such measurements other inputs from radio measurements of circular polarization that are sensitive to the line-of-sight component of the coronal magnetic field or high resolution high dynamic range quiet sun radio imaging Mercier *et al.* (2006) of the sun at low frequencies will also be very useful.

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